## SK2411, IO2659 VT2009 Exam tasks

Task 1.

- (a) Prove formally that the maximum four-level laser efficiency (ratio of the laser output power to the pump power), when the laser is operating far above the threshold  $\left(\frac{P_{pump}}{P_{th}} \gg 1\right)$  depends only on the laser and pump photon energies and the pumping efficiency. For simplicity consider longitudinal pumping with perfect beam matching between the pump and laser mode  $(w_0 = w_p)$ . The maximum efficiency also implies that there are no other losses except for those due to output coupling. (3 points)
- (b) There are two lasers generating 100 W output power each and operating under maximum efficiency conditions and with maximum pumping efficiency:
- (i) Nd:YAG pumped at 808 nm and generating radiation at 1064 nm,
- (ii)Yb:YAG pumped at 940 nm and generating radiation at 1040 nm

Calculate the heat power produced by these lasers. (1 point)

Task 2.

- (a)Which laser diode structure, homojunction or heterojunction has lower threshold current density and why? (1 point)
- (b) What is natural linewidth? What determines it? (1 point)
- (c) You have a choice of two laser gain materials, Nd:YAG and Nd:glass, and need to make a laser at the peak of four-level transition spectral line. Homogeneously broadened linewidth in Nd:YAG is 13.5 GHz and upper laser level lifetime is 230  $\mu$ s. The same transition in Nd:glass is inhomogeneously broadened to 5.4 THz and the upper laser level lifetime is 300  $\mu$ s. Which material would provide smaller laser threshold and how many times considering that cavity losses are the same in both cases? (2 points)

Task 3.



- Which scheme would be suitable for making a continuous wave laser for transitions between u and l levels, assuming that the transitions u-l, l-g are dipole-allowed and have equal transition dipole matrix elements, while the transition u-g is dipole-forbidden? Motivate your answer. (1 point).
- (b) Semiconductor chip manufacturer has given you a task to find a suitable laser technology for lithography used in manufacturing next generation chips with the smallest feature size of 100 nm. Which laser type would you choose and why? (1 point).
- (c) Rotational-vibrational absorption and emission spectrum consists of series of lines attributed to P, and R branches. Take for instance a P branch of the absorption which corresponds to transitions J''=J'-1 (see Figure below) and prove that the separation of absorption and emission lines in frequency is equidistant, i.e. the frequency separation between adjacent spectral lines in the rotational-vibrational spectrum remain the same, regardless of the initial rotational quantum number J'. (2 points)



Task 4.

- (a) What is the Rayleigh range of a Gaussian beam? (1 point)
- (b) For a ray entering a spherical dielectric interface from a medium of refractive index  $n_1$  to a medium of refractive index  $n_2$ , with radius of curvature R (assume R>0 if the center of curvature is to the left of the surface), the ABCD matrix is  $\begin{bmatrix} 1 & 0 \\ \frac{n_2 n_1}{n_2 R} & \frac{n_1}{n_2} \end{bmatrix}$ . The ABCD matrix for a thin lens is  $\begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix}$ . Calculate the ABCD matrix of a spherical lens, made up of two closely spaced dielectric interfaces, of radii  $R_1$  and  $R_2$ , enclosing a material of refractive index  $n_2$ . The lens is immersed in a medium of refractive index  $n_1$ . Derive the expression of f using  $R_1$  and  $R_2$ . (1 point)
- (c) A given He-Ne laser oscillating in a pure Gaussian  $\text{TEM}_{00}$  mode at  $\lambda$ =632.8 nm with an output power of *P*=5 mW has a far-field divergence-angle of 1 mrad. Calculate spot size and peak intensity at the waist position. (2 points).

Task 5.

Consider the optical pumping system.

- (a) What is longitudinal pumping? What is transverse pumping? (1 point)
- (b) Describe the pumping efficiency, and four main terms contributing to the pumping efficiency. Explain why diode laser pumping is more efficient than lamp pumping. (1 point)
- (c) Consider a rod-shaped active medium pumped by a laser beam, and let *z* be the longitudinal coordinate along the rod axis. *r* is the radial distance from the rod axis. Prove that, for longitudinal pumping, the pump rate is  $R_p(r,z)=\alpha I_p(r,z)/hv_p$ , where  $I_p(r,z)$  is the pump intensity in the active medium and  $\alpha$  is the absorption coefficient at the frequency  $v_p$  of the pump. (2 points)

## Task 6.

- (a) Write down the space independent rate equations for a quasi-three level system, and explain the physical meaning of each parameter and the equation itself. (1 point)
- (b) Derive the critical pumping rate from the above rate equations. (1 point)
- (c) Calculate the population inversion necessary to achieve CW laser oscillation in a ruby laser (quasi-three level system) at the wavelength  $\lambda$ =694.3 nm. Assume a Fabry-Perot resonator with mirror reflectivity 100% and 96%, a scattering loss of 3% per round trip, and a 6 cm long ruby rod. Assume also equal values for absorption and stimulated emission peak cross sections  $\sigma_a = \sigma_e = 2.7 \times 10^{-20}$  cm<sup>2</sup>. (1 point)
- (d) Assume the above laser is operating at the transient mode through mode locking. If the bandwidth of the laser transition for the above laser is 11 cm<sup>-1</sup> (in the unit of wave-number) and the mode amplitude spectrum has a Gaussian shape, calculate the pulse width. (1 point)